Reading Quiz #2

Name: _____ Class: _____ Student I.D. #_____

Read Sections 2.4-2.8(pages 113-171) and work out the following problems.

122.35 For what value of the constant c is the function f continuous on $(-\infty, \infty)$, where

$$f(x) = \begin{cases} cx^2 + 2x & \text{if } x < 2\\ x^3 - cx & \text{if } x \ge 2 \end{cases}$$

122.53 Show that the function f is continuous on $(-\infty,\infty),$ where

$$f(x) = \begin{cases} x^4 \sin \frac{1}{x} & \text{if } x \neq 0\\ 0 & \text{if } x = 0 \end{cases}$$

133.27 Find the limit $\lim_{x\to\infty}(\sqrt{9x^2+x}-3x)$

134.39 Find the horizontal and vertical asymptotes of the curve $y = \frac{2x^2 + x - 1}{x^2 + x - 2}$

143.35 The limit $\lim_{x\to 5} \frac{2^x - 32}{x-5}$ represents the derivative of some function f at some point a. State such an f and a.

145.54 Determine whether f'(0) exists, if

$$f(x) = \begin{cases} x^2 \sin \frac{1}{x} & \text{if } x \neq 0\\ 0 & \text{if } x = 0 \end{cases}$$

156.25 Find the derivative of the function $g(x) = \sqrt{1+2x}$ using the definition of derivative. State the domain of the function and state the domain of the derivative.

163.28 Let $f(x) = x^4 - 2x^2$

- (a) Use the definition of derivative to find f'(x) and f''(x)
- (b) On what intervals is f increasing or decreasing
- (c) On what intervals is f concave upward or concave downward