

# 微積分A下(統計系)預習測驗 #12

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預習第16章第4節(pp. 1040-1043), 然後回答下列問題

1. The polar coordinates  $(r, \theta)$  of a point are related to the rectangular coordinates  $(x, y)$  by the equations (page 1040)

2. If  $f$  is continuous on a polar rectangle  $R$  given by  $0 \leq a \leq r \leq b$ ,  $\alpha \leq \theta \leq \beta$ , where  $0 \leq \beta - \alpha \leq 2\pi$ , then (page 1041)

$$\iint_R f(x, y) dA =$$

3. If  $f$  is continuous on a polar region  $D$  given by  $\alpha \leq \theta \leq \beta$ ,  $r_1(\theta) \leq r \leq r_2(\theta)$ , then (page 1042)

$$\iint_R f(x, y) dA =$$

4. Sketch the graph of the polar equation  $r = \cos 2\theta$ .

(a) Fill in all blanks in the following table.

$\theta$	0	$\pm \frac{\pi}{12}$	$\pm \frac{\pi}{8}$	$\pm \frac{\pi}{6}$	$\pm \frac{\pi}{4}$	$\pm \frac{\pi}{3}$	$\pm \frac{3\pi}{8}$	$\pm \frac{5\pi}{12}$	$\pm \frac{\pi}{2}$
$2\theta$	0								
$r = \cos 2\theta$	1								
$\theta$	0	$\pm \frac{7\pi}{12}$	$\pm \frac{5\pi}{8}$	$\pm \frac{2\pi}{3}$	$\pm \frac{3\pi}{4}$	$\pm \frac{5\pi}{6}$	$\pm \frac{7\pi}{8}$	$\pm \frac{11\pi}{12}$	$\pm \pi$
$2\theta$	0								
$r = \cos 2\theta$	1								

(b) Plot all these points  $(r, \theta)$  and sketch the graph of the polar equation  $r = \cos 2\theta$ .